

Nacher-Modell
für $D=0, \varepsilon=0$

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$$\begin{aligned} \delta_R \rightarrow x \rightarrow \delta_D(t) &= \delta_D + w\dot{x} = \delta_R - \delta_D(t) \cdot x \\ &= \delta_D + w(t) \\ \langle ww \rangle &= 2\eta \delta(\tau) \end{aligned}$$

Def: $w(t) = \sqrt{2\eta} \Omega(t)$

$$\Rightarrow \langle ww \rangle = \langle \sqrt{2\eta} \Omega \cdot \sqrt{2\eta} \Omega \rangle = (2\eta) \langle \Omega \Omega \rangle$$

$$\langle ww \rangle = (2\eta) \delta(\tau)$$

$$\Rightarrow \langle \Omega \Omega \rangle = \delta(\tau) \quad \checkmark$$

Somit: $\dot{x} = \delta_R - (\delta_D + \sqrt{2\eta} \Omega(t)) x$

$$\dot{x} = \underbrace{[\delta_R - \delta_D x]}_f + \underbrace{[-\sqrt{2\eta} x]}_g$$

$$g^2 = 2\eta x^2 \Rightarrow \frac{d}{dx} g^2 = 4\eta x$$

$$A(x) = \delta_R - \delta_D x + \frac{\varepsilon}{4} 4\eta x = \delta_R + (\varepsilon\eta - \delta_D) x$$

$$B(x) = \frac{1}{2} \cdot 2\eta x^2 = \eta x^2$$

$$\left. \begin{aligned} A(x \rightarrow \infty) &\rightarrow (\varepsilon\eta - \delta_D) x \\ B(x \rightarrow \infty) &\rightarrow \eta x^2 \end{aligned} \right\} \Rightarrow I(x \rightarrow \infty) \rightarrow \left(\frac{\varepsilon\eta - \delta_D}{\eta} \right) \int_{x_{\min}}^x s^{-1} ds$$

$$\Rightarrow \exp[I(x \rightarrow \infty)] = (x/x_{\min})^{\varepsilon - (\delta_D/\eta)} \quad \ln(x/x_{\min})$$

$$\Rightarrow P(x \rightarrow \infty) \rightarrow \frac{\mathcal{N}}{\eta} x^{-2} (x/x_{\min})^{\varepsilon - (\delta_0/\eta)}$$

$$= \left(\frac{\mathcal{N} x_{\min}^{-2}}{\eta} \right) \underbrace{(x/x_{\min})^{-2} (x/x_{\min})^{\varepsilon - (\delta_0/\eta)}}_{(x/x_{\min})^{\varepsilon - 2 - (\delta_0/\eta)}}$$

Somit: $P(x \rightarrow \infty) \rightarrow x^{[\varepsilon - 2 - (\delta_0/\eta)]}$

Das Resultat aus dem Nacher-Paper ergibt sich für $\varepsilon = +1$.

Dann gilt $P \sim x^{1 - 2 - (\delta_0/\eta)} \sim x^{-1 - (\delta_0/\eta)}$
 $\sim x^{-(1 + \frac{\delta_0}{\eta})} \checkmark$